

Package: rineq (via r-universe)

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Title Concentration Index and Decomposition for Health Inequalities

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Description Relative, generalized, and Erreygers corrected concentration index; plot Lorenz curves; and decompose health inequalities into contributing factors. The package currently works with (generalized) linear models, survival models, complex survey models, and marginal effects probit models. originally forked by Brecht Devleesschauwer from the 'decomp' package (no longer on CRAN), 'rineq' is now maintained by Kaspar Walter Meili. Compared to the earlier 'rineq' version on 'github' by Brecht Devleesschauwer (<https://github.com/brechtdev/rineq>), the regression tree functionality has been removed. Improvements compared to earlier versions include improved plotting of decomposition and concentration, added functionality to calculate the concentration index with different methods, calculation of robust standard errors, and support for the decomposition analysis using marginal effects probit regression models. The development version is available at <https://github.com/kdevkdev/rineq>.

Depends R (>= 3.5.0)

Imports stats, graphics

Suggests sandwich, lmtest, mfx, survey, survival

License GPL (>=2)

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Repository <https://kdevkdev.r-universe.dev>

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ci	<i>Calculates different type of concentration indexes</i>
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Description

This function calculates the relative concentration index (Kakwani et al.), the generalized concentration index (Clarke et al., 2002), the Wagstaff index for bounded variables (Owen et al. 2016), and the concentration index with Erreygers' correction (Erreygers et al., 2009). It returns an object of class hci for which confidence intervals, summaries and plots are defined.

Usage

```
ci(
  ineqvar,
  outcome,
  weights = NULL,
  type = c("CI", "CIg", "CIc", "CIw"),
  method = c("linreg_delta", "linreg_convenience", "cov_convenience", "direct"),
  df_correction = TRUE,
  robust_se = FALSE,
  rse_type = "HC3",
  rank_function = rineq::rank_wt
)
```

Arguments

ineqvar	Used for ranking, usually relates to the socioeconomic position, for example income.
outcome	The variable in which the inequality should be measures, for example health.
weights	Optional, used to weigh the observations. Defaults to equal weights for all observations.
type	Character, the type of concentration index to be calculated: relative concentration index (CI, default), generalized concentration index (CIg), concentration index with Erreygers Correction CIc, or Wagstaff concentration index suitable for bounded and binary outcomes CIw
method	Character, defines the calculation method. One of: <ul style="list-style-type: none"> • <code>linreg_delta</code>: Based on linear regression without transforming the left hand side variable. Computes correct standard errors that take into account the sampling variability of the estimate of the mean (O'Donnell et al. 2008, Owen et al. 2016) • <code>linreg_convenience</code>: Based on simpler regression with transformed left hand side variable. Standard errors do not take into account the sampling variability of the estimate of the mean(O'Donnell et al. 2008, Owen et al. 2016) • <code>cov_convenience</code>: Based on covariance. Equivalent to <code>linreg_convenience</code> (O'Donnell et al. 2008, Owen et al. 2016) • <code>direct</code>: Using direct formula, standard errors do no take weighting appropriately into account (O'Donnell et al. 2008, Kakwani et al. 1997)
df_correction	If TRUE (default), calculates the concentration index based on the population variance (derived from the sample variance).
robust_se	Uses robust standard errors if TRUE. Only available for the <code>linreg_*</code> type methods. Requires the <code>sandwich</code> package.
rse_type	Character, type argument for the <code>vcovHC()</code> . HC3' is suggested as default, set to HC1 for Stata compatibility. See <code>?sandwich::vcovHC()</code> for options.
rank_function	Function to calculate the weighted rank of <code>ineqvar</code> . Takes two arguments: the variable that holds the rank order information, and the weights for the ranks. <code>rineq</code> currently provides two, <code>rank_wt</code> (default, corresponds to code provided in the World Bank report by O'Donnell et al.,2008) and <code>rank_gwt</code> (generalized handling of ties as also used by the Stata <code>Conindex</code> command, initially published by van Ourti, (2004)).

Value

An S3 object of class `hci`. Contains:

- `concentration_index` The concentration index
- `type` The type
- `method` The method used for calculation
- `variance` The variance,used for calculation of confidence intervals

- fractional_rank Computed fractional rank NA
- outcome Outcome after removing NA
- call Call signature
- n Number of observations after removing NA
- robust_se Were robust standard errors calculated?
- rse_type Type of robust standard errors.
- df_correction Do the degrees of freedom correspond to a sample?

References

- Clarke, P. M., Gerdtham, U. G., Johannesson, M., Binglefors, K., & Smith, L. (2002). On the measurement of relative and absolute income-related health inequality. *Social Science & Medicine*, 55(11), 1923-1928
- Erreygers, G. (2009). Correcting the concentration index. *Journal of health economics*, 28(2), 504-515
- Kakwani, N., Wagstaff, A., & Van Doorslaer, E. (1997). Socioeconomic inequalities in health: measurement, computation, and statistical inference. *Journal of econometrics*, 77(1), 87-103.
- O'Donnell, O., O'Neill S., Van Ourti T., & Walsh B. (2016). Conindex: Estimation of Concentration Indices. *The Stata Journal*, 16(1): 112-138.
- O'Donnell, O., Van Doorslaer, E., Wagstaff, A., Lindelow, M., 2008. *Analyzing Health Equity Using Household Survey Data: A Guide to Techniques and Their Implementation*, World Bank Publications. The World Bank.
- van Ourti, T., 2004. Measuring horizontal inequity in Belgian health care using a Gaussian random effects two part count data model. *Health Economics*, 13: 705-724.

Examples

```
# Direct
data(housing)
ci.bmi <- ci(ineqvar = housing$income, outcome = housing$bmi, method = "direct")
summary(ci.bmi)

# retrieve value
ci.bmi$concentration_index

# obtain confidence intervals
confint(ci.bmi, level = 0.95)

plot(ci.bmi)

# Wagstaff type with binary outcome and robust standard errors
# that should correspond to Stata (depends on 'sandwich'):

ci.bmi.b <- ci(housing$income, housing$high.bmi, type = "CIw", robust_se = TRUE,
  rse_type = "HC1")
```

confint.hci	<i>Confidence intervals for hci objects</i>
-------------	---

Description

Confidence intervals for hci objects

Usage

```
## S3 method for class 'hci'
confint(object, parm = NULL, level = 0.95, ...)
```

Arguments

object	An object of class hci
parm	Unused
level	Confidence interval level defaults to 0.95
...	Unused

Value

A confidence interval in a numeric vector of length 2

Examples

```
data(housing)
ci.bmi <- ci(ineqvar = housing$income, outcome = housing$bmi, method = "direct")
confint(ci.bmi)
```

contribution	<i>Function to decompose the Relative Concentration Index into its components</i>
--------------	---

Description

Currently compatible with lm, glm logit and probit, svyglm, coxph and mfx marginal effects probit.

Usage

```
contribution(object, ranker, correction = TRUE, type = "CI", intercept = "exclude")
```

Arguments

object	The model result object. class <code>coxph</code> , <code>glm</code> , <code>lm</code> or <code>svyglm</code> , <code>probitmfx</code> , <code>logitmfx</code> ; the outcome should be the health variable and the predictors the components.
ranker	Ranking variable with the same length as the outcome.
correction	A logical indicating whether the global and partial confidence should be corrected for negative values using imputation.
type	Character, concentration index type that the decomposition should be applied to. Defaults to CI. Use CIw for binary outcomes.
intercept	Character, one of <code>exclude</code> or <code>include</code> , defaults to <code>exclude</code> . If <code>exclude</code> , the intercept coefficient will not included in the decomposition analysis, if set to <code>include</code> , it will be included.

Details

These functions decompose the Relative Concentration Index into its components using a (generalized) linear model, optionally using a survey design, or a Cox Proportional Hazards model. `Print`, `summary` and `plot` methods have been defined for the results.

If `correction` is `TRUE` negative values of components or outcome are corrected using `correct_sign()` with option `shift = FALSE`.

For non-linear models the decomposition needs to rely on a linear approximations of the effects. There are different approaches. One is to work on the scale of the `glm` coefficients and calculate the concentration index based on the predicted outcome. (Konings et al., 2010, Speybroeck et al., 2010). Another approach is to use marginal effects as beta coefficients and the original outcome (O'Donnel et al. 2008).

This function supports both. For `glm`, `coxph`, and `svyglm` models, the first approach is used. The second approach is implemented for model objects of type `probitmfx` and `logitmfx` from the 'mfx' package. See examples.

Per default, the intercept in models is excluded, but this can be changed by setting the the `intercept` argument to `include`, but this may conceptually make less sense and is more appropriate if the model does not contain an intercept.

Use `decomposition()` function directly to manually specify coefficients, outcomes, and model matrices for arbitrary models.

NOTE: Only models with data with ordinary indexes are supported (starting from 1, sequentially increasing by increments of 1). For the case were rows with NA are automatically omitted by the model function, the used indices are guessed based on the row names of the model matrix and then used for accessing the ranker variable. However, this may lead to issues if the row names do not correspond to ordinary integer indexes.

Value

An object of class `decomposition` containing the following components:

- `betas` A numeric vector containing regression coefficients
- `partial_cis` A numeric vector containing partial confidence intervals
- `confints` A numeric vector containing 95\

- averages Weighted averages of every variable in the model
- ci_contribution Confidence intervals for contributions
- overall_ci Confidence intervals for the concentration index
- corrected_coefficients Corrected coefficients using `correct_sign()` if, requested FALSE otherwise
- outcome_corrected Corrected outcome `correct_sign()` if requested, FALSE otherwise
- rows Rownames of used rows in the model

Warning

ranker should be chosen with care. Ideally, it is a variable from the same dataframe as the other variables. If not, redefine the row names in the model.

Author(s)

Peter Konings

References

Konings, P., Harper, S., Lynch, J., Hosseinpoor, A.R., Berkvens, D., Lorant, V., Geckova, A., Speybroeck, N., 2010. Analysis of socioeconomic health inequalities using the concentration index. *Int J Public Health* 55, 71–74. <https://doi.org/10.1007/s00038-009-0078-y>

Speybroeck, N., Konings, P., Lynch, J., Harper, S., Berkvens, D., Lorant, V., Geckova, A., Hosseinpoor, A.R., 2010. Decomposing socioeconomic health inequalities. *Int J Public Health* 55, 347–351. <https://doi.org/10.1007/s00038-009-0105-z>

O'Donnell, O., Doorslaer, E. van, Wagstaff, A., Lindelow, M., 2008. *Analyzing Health Equity Using Household Survey Data: A Guide to Techniques and Their Implementation*, World Bank Publications. The World Bank.

Examples

```
data(housing)

## Linear regression direct decomposition
fit.lm <- lm(bmi ~ sex + tenure + place + age, data = housing)

# decompose relative concentration index
contrib.lm <- contribution(fit.lm, housing$income)
summary(contrib.lm)
plot(contrib.lm, decreasing = FALSE, horiz = TRUE)

# GLM: Decomposition based on predicted outcome
fit.logit <- glm(high.bmi ~ sex + tenure + place + age, data = housing)

contrib.logit <- contribution(fit.logit, housing$income)
summary(contrib.logit)
plot(contrib.logit, decreasing = FALSE, horiz = TRUE)
```

```

# GLM probit: Decomposition based on predicted outcome
fit.probit <- glm(high.bmi ~ sex + tenure + place + age, data = housing,
                 family = binomial(link = probit))

# binary, set type to 'CIw'
contrib.probit <- contribution(fit.probit, housing$income, type = "CIw")
summary(contrib.probit)
plot(contrib.probit, decreasing = FALSE, horiz = TRUE)

# Marginal effects probit using package 'mfx': Decomposition based on predicted outcome
fit.mfx <- mfx::probitmfx(high.bmi ~ sex + tenure + place + age, data = housing)

contrib.mfx <- contribution(fit.mfx, housing$income, type = "CIw")
summary(contrib.mfx, type="CIw")
plot(contrib.mfx, decreasing = FALSE, horiz = TRUE)

# package survey svy
des = survey::svydesign(~1, data= housing, weights = rep(1, NROW(housing)))
fit.svy = survey::svyglm(bmi ~ tenure+height+weight, design = des)
contrib.svy = contribution(fit.svy, housing$income)

# adopted from the `coxph` example in survival package
testcph <- data.frame(time = c(4,3,1,1,2,2,3),
                     status = c(1,1,1,0,1,1,0),
                     x = c(0,2,1,1,1,0,0),
                     sex = c(0,0,0,0,1,1,1),
                     income = c(100,50, 20, 20, 50, 60,100))

# Fit a stratified model
fit.coxph = survival::coxph(survival::Surv(time, status) ~ x + survival::strata(sex), testcph)
contrib.coxph = contribution(fit.coxph, testcph$income)

```

correct_sign

Corrects negative values in the health variable

Description

The Relative Concentration Index is not bonded between $[-1, 1]$ if the health variable contains both negative and positive values. This function corrects for this either by imputing a value of 0 for all negative values or by subtracting the minimum value.

Usage

```
correct_sign(x, shift = TRUE)
```



```
corrected_value(x)
```

```
is_corrected(x)
```

Arguments

x	A numeric vector, typically representing health.
shift	If FALSE (the default), 0 is imputed for all negative values in x. If TRUE the minimum value of x is subtracted from it.

Value

correct_sign() returns a list with 2 components:

corrected corrected version of x

modified logical, TRUE when any of the elements of x have been changed

corrected_value() returns the corrected value if passed the result of 'correct_sign()'.
is_corrected() returns TRUE if a modifications was made if passed the result of correct_sign(), FALSE otherwise.

These components can be extracted with the functions corrected_value and is_corrected.

Functions

- corrected_value(): Return the corrected value
- is_corrected(): Check if the sign was corrected

Author(s)

Peter Konings

Examples

```
data("housing")

# standardize & normalize bmi, will introduce negative values
housing$bmi.std <- (housing$bmi - mean(housing$bmi))/ sd(housing$bmi)

housing$bmi.std.shifted <- corrected_value(correct_sign(housing$bmi.std, shift = TRUE))
housing$bmi.std.imputed <- corrected_value(correct_sign(housing$bmi.std, shift = FALSE))

## compare the effect of both methods
plot(density(housing$bmi.std, na.rm = TRUE))
points(density(housing$bmi.std.shifted, na.rm = TRUE), col = 'blue')
points(density(housing$bmi.std.imputed, na.rm = TRUE), col = 'green')
```

 decomposition

Decomposition analysis

Description

Used by the wrapper `contribution()` but can be used manually. Calculates the decomposition for a given regression model.

Usage

```
decomposition(outcome, betas, mm, ranker, wt, correction, citype = "CI")
```

Arguments

outcome	Outcome variable
betas	Beta coefficients from regression.
mm	Model matrix from regression
ranker	Ranking variable
wt	Weights
correction	Apply sign correction?
citype	Character, CI type to be calculated, defaults to CI. Use CIw for binary outcomes.

Details

NOTE: Only models with data with ordinary indexes are supported (starting from 1, sequentially increasing by increments of 1). For the case where rows with NA are automatically omitted by the model function, the used indices are guessed based on the row names of the model matrix and then used for accessing the ranker variable. However, this may lead to issues if the row names do not correspond to ordinary integer indexes.

Value

S3 object of class decomposition

Examples

```
fit.lm = lm(mtcars$mpg ~ mtcars$cyl)
decomp = decomposition(mtcars$mpg, coefficients(fit.lm), fit.lm$model,
                      mtcars$hp, wt = rep(1, nrow(mtcars)), correction = FALSE)
summary(decomp)
```

housing	<i>Artificial example data on housing conditions</i>
---------	--

Description

Microdata with a permissive license that includes continuous data on health and income is hard to come by. In stead of real data, the package thus includes an imaginary dataset.

Usage

```
data(housing)
```

Format

data.frame object.

Variable list:

id unique identifier per person

sex female or male

age integer, from 20 to 94

tenure categorical. One of homeless, irregular, own_apartment, own_house, or rent

height height in cm

weight weight in kg

bmi $\text{weight}/(\text{height}/100)^2$

income continuous, imaginary currency without unit

Source

Artificially generated by the package authors

plot.decomposition	<i>Plots a barplot of the contribution percentages in a decomposition object. Sets custom plot margins and uses the graphical parameters xlim, horiz, las and xlab which therefore cannot be customized</i>
--------------------	---

Description

Plots a barplot of the contribution percentages in a decomposition object. Sets custom plot margins and uses the graphical parameters xlim, horiz, las and xlab which therefore cannot be customized

Usage

```
## S3 method for class 'decomposition'
plot(x, decreasing = TRUE, horiz = FALSE, ...)
```

Arguments

x	Object returned from decomposition function
decreasing	Whether to sort contributions decreasing or not
horiz	If the barplots should be printed horizontally or vertically
...	Graphical parameter passed on to base::barplot()

Value

Invisibly returns x as the function is called for side effects (plotting).

Examples

```
data(housing)
# Linear regression & decompose
fit.lm <- lm(bmi ~ sex + tenure + place + age, data = housing)
contrib.lm <- contribution(fit.lm, housing$income)

# plot horizontally, in increasing order
plot(contrib.lm, decreasing = FALSE, horiz = TRUE)
```

plot.hci

Plots the concentration curve for an hci object.

Description

Plots the concentration curve for an hci object.

Usage

```
## S3 method for class 'hci'
plot(x, ...)
```

Arguments

x	Object with of hci
...	Further arguments passed to base::plot()

Value

Invisibly returns x as the function is called for side effects (plotting).

Examples

```
data(housing)
ci.bmi <- ci(ineqvar = housing$income, outcome = housing$bmi, method = "direct")
plot(ci.bmi)
```

print.decomposition *Print function for decomposition objects.*

Description

Print function for decomposition objects.

Usage

```
## S3 method for class 'decomposition'  
print(x, ...)
```

Arguments

x	Object of type decomposition
...	Currently unused

Value

Invisibly returns x as the function is called for side effects.

Examples

```
data(housing)  
# Linear regression & decompose  
fit.lm <- lm(bmi ~ sex + tenure + place + age, data = housing)  
contrib.lm <- contribution(fit.lm, housing$income)  
  
# print  
print(contrib.lm)
```

print.hci *Prints an hci object.*

Description

Prints an hci object.

Usage

```
## S3 method for class 'hci'  
print(x, ...)
```

Arguments

x	Object of type hci
...	Currently unused

Value

Invisibly returns x as the function is called for side effects.

Examples

```
data(housing)
ci.bmi <- ci(ineqvar = housing$income, outcome = housing$bmi, method = "direct")
print(ci.bmi)
```

rank_gwt

Generalized weighted ranking function

Description

In the case of ties, the ordinary `rank_wt()` function uses the order in the original data. This is the same approach as in the stata code provided by O'Donnell et al. (2008) in the original World Bank publication, but depends on the arbitrary initial order in the data. The Stat conindex code however uses the generalized weighted rank implementation published by van Ourti (2004). For Stata compatibility use `rank_gwt()`

Usage

```
rank_gwt(x, wt)
```

Arguments

<code>x</code>	numeric vector
<code>wt</code>	weights

Details

The formula notation in van Ourti (2004) seems to rely on absolute an absolute deduction of 1 unit of monetary income value. This only works in the integer case. Instead, this this implementation uses the next lowest x value, respectively the next lowest rank, to calculate the proportion of the inequality variable up to the respective value

Value

A numeric vector containing weighted fractional ranks of the elements of x .

References

van Ourti, T., 2004. Measuring horizontal inequity in Belgian health care using a Gaussian random effects two part count data model. *Health Economics*, 13: 705–724.

Examples

```
x <- sample(1:10, size = 10, replace = TRUE)
x.weight <- seq(0, 1, length.out = 10)
rank_gwt(x, wt = x.weight)
```

rank_wt	<i>Calculates the weighted rank</i>
---------	-------------------------------------

Description

Calculates the weighted rank

Usage

```
rank_wt(x, wt)
```

Arguments

x	numeric vector
wt	weights

Value

A numeric vector containing weighted fractional ranks of the elements of x.

Author(s)

Peter Konings

References

Kakwani *et al.*, 1997.

Examples

```
x <- sample(1:10, size = 10, replace = TRUE)
x.weight <- seq(0, 1, length.out = 10)
rank_wt(x, wt = x.weight)
```

```
summary.decomposition Prints and returns a summary for a decomposition object.
```

Description

Prints and returns a summary for a decomposition object.

Usage

```
## S3 method for class 'decomposition'
summary(object, digits = getOption("digits"), addcoefs = FALSE, ...)
```

Arguments

object	Result of a decomposition analysis, of class decomposition
digits	Number of digits, defaults to R digits option
addcoefs	Whether or not to add coefficients (defaults to FALSE)
...	Additional parameters, currently unused

Value

A data frame with columns for the absolute and relative contribution, elasticity, concentration index including confidence intervals, and whether correction was applied. If specified using addcoefs, the coefficients are included as the first column.

Examples

```
data(housing)
# Linear regression & decompose
fit.lm <- lm(bmi ~ sex + tenure + place + age, data = housing)
contrib.lm <- contribution(fit.lm, housing$income)

# print
print(contrib.lm)
```

```
summary.hci Prints the a summary of the concentration index object hci
```

Description

Prints the a summary of the concentration index object hci

Usage

```
## S3 method for class 'hci'
summary(object, ...)
```


Arguments

object	Object of type hci
...	Currently unused

Value

No returns value. Directly prints to the standard output connection.

Examples

```
data(housing)
ci.bmi <- ci(ineqvar = housing$income, outcome = housing$bmi, method = "direct")
summary(ci.bmi)
```

var_wt	<i>Calculates the weighted variance</i>
--------	---

Description

Calculates the weighted variance

Usage

```
var_wt(x, wt, na.rm = FALSE)
```

Arguments

x	numeric vector
wt	weights
na.rm	If TRUE, indices where x is NA will be removed

Value

A numeric vector containing weighted variance of the elements of x

Examples

```
x <- sample(1:10, size = 10, replace = TRUE)
x.weight <- seq(0, 1, length.out = 10)
var_wt(x, wt = x.weight)
```

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